Counting Combinations

Boise Math Circle

Big Idea

If order doesn't matter, how many ways are there to choose a fixed number of items from a set of objects?

Example

Joe has 5 friends (Abe, Billy, Charlie, Danny, Evan) and needs to pick 3 friends to be his "besties". How may combinations are possible? (list them below)

Note: When we count these, mathematicians say "5 choose 3" and write $\begin{pmatrix} 5\\3 \end{pmatrix}$.

Compute the following:

$$\begin{pmatrix} 7\\3 \end{pmatrix} = \begin{pmatrix} 10\\3 \end{pmatrix} = \begin{pmatrix} 26\\3 \end{pmatrix} =$$

Write a formula for each of the following:

$$\binom{n}{3} = \binom{n}{5} = \binom{n}{k} =$$

Pascal's Triangle for Combinations



Good Questions about Combinations

- Why should "10 choose 2" be the same as "10 choose 8"?
- Can you express the combination formula using just factorials?
- Explain the following pattern: The number of ways to pick 3 people from 10 people is the same as the total number of ways to pick 2 or 3 people from 9 people.
- Explain the following pattern: The sum of each row is a power of 2.